

Enhancing ASP with Constraints - The OrderLib

Max Ostrowski

University of Potsdam

Outline

1 General Theory Language

2 SAT Modulo Theories

3 OrderLib

4 Example Evaluation

Overview

1 General Theory Language

2 SAT Modulo Theories

3 OrderLib

4 Example Evaluation

Introduction

- combining ASP with any kind of theory
- SMT (SAT modulo Theories)
- LA, LIA, LRA, RA, Arrays, EUF, DL, Bitvectors, ...

A General Theory Language

Advantages

- no need to change the grounder gringo
- reuse of grounding capabilities to instantiate theory terms
- extensible to any theory
- basic syntax checking in the frontend
- AST and interface for writing your theory solver

A General Theory Language

Theory Atom

`&name { theory terms : condition } <op> theory term.`

syntax is similar to aggregates

A General Theory Language

Theory Atom

`&name { theory terms : condition } <op> theory term.`

syntax is similar to aggregates

A General Theory Language

ASP modulo Acyclicity

```
1 { path(X,Y) : edge(X,Y) } 1 :- node(X).  
1 { path(X,Y) : edge(X,Y) } 1 :- node(Y).  
start(X) :- X = #min { Y : node(Y) }.  
&edge { X,Y } :- path(X,Y), not start(Y).
```

A General Theory Language

ASP modulo Acyclicity

```
1 { path(X,Y) : edge(X,Y) } 1 :- node(X).  
1 { path(X,Y) : edge(X,Y) } 1 :- node(Y).  
start(X) :- X = #min { Y : node(Y) }.  
&edge { X,Y } :- path(X,Y), not start(Y).
```

A General Theory Language

ASP modulo Heuristics

```
&heuristic { atom(X,Y), [sign,0,0] : cond(X,Y) }.
```

A General Theory Language

ASP modulo Preferences

```
&preference(p1,subset) {  
a(X) : gr(X);  
b(X) : gr(X)  
}.  
  
&preference(p2,lexico) {  
(1,X) :: name(X) : preference(X)  
}.  
  
&preference(p3,aso) {  
a(X) > ~b(Y) || c(Z) & ~d(W) : dom(a,X;b,Y;c,Z;d,W)  
}.
```

A General Theory Language

ASP modulo CSP

```
p(1..10).  
q(X,1,10) :- p(X).  
&dom {  
  f(X) :: {1..3, 5..7} : p(X);  
  g(X) :: {L..U} : q(X,L,U);  
  1 <= x <= 10  
}.  
&show { f/1 }.  
a :- &sum{ X * f(X) + g(Y) : X=1..3 } >= 42, p(Y).
```

A General Theory Language

ASP modulo CSP

```
p(1..10).  
q(X,1,10) :- p(X).  
&dom {  
  f(X) :: {1..3, 5..7} : p(X);  
  g(X) :: {L..U} : q(X,L,U);  
  1 <= x <= 10  
}.  
&show { f/1 }.  
a :- &sum{ X * f(X) + g(Y) : X=1..3 } >= 42, p(Y).
```

A General Theory Language

ASP modulo CSP

```
p(1..10).  
q(X,1,10) :- p(X).  
&dom {  
  f(X) :: {1..3, 5..7} : p(X);  
  g(X) :: {L..U} : q(X,L,U);  
  1 <= x <= 10  
}.  
&show { f/1 }.  
a :- &sum{ X * f(X) + g(Y) : X=1..3 } >= 42, p(Y).
```

A General Theory Language

Language Specification for ASPmCSP

```
#theory csp {  
  linear_term {  
    + : 1, unary;  
    - : 1, unary;  
    * : 2, binary, left;  
    + : 3, binary, left;  
    - : 3, binary, left  
  };  
  ...  
}
```

A General Theory Language

Language Specification for ASPmCSP

```
domain_term {
  <= : 1, binary, left;
  >= : 1, binary, left;
  > : 1, binary, left;
  < : 1, binary, left;
  = : 1, binary, left;
  != : 1, binary, left;
  :: : 1, binary, left };
show_term { / : 1, binary, left};
&dom/0 : domain_term, directive;
&show/0 : show_term, directive;
&sum/0 : linear_term, { <=, >=, <, >, =, != },
        linear_term, any
}.
```

Overview

1 General Theory Language

2 SAT Modulo Theories

3 OrderLib

4 Example Evaluation

Techniques

- early approach
- lazy approach
- online approach
 - incremental (lazy clause generation)
 - theory propagation
 - lazy variable creation

Techniques

- early approach
- lazy approach
- online approach
 - **incremental** (lazy clause generation)
 - **theory propagation**
 - lazy variable creation

clingcon

Techniques

- early approach
- lazy approach
- online approach
 - incremental (lazy clause generation)
 - theory propagation
 - lazy variable creation

orderLib

Overview

1 General Theory Language

2 SAT Modulo Theories

3 OrderLib

4 Example Evaluation

Translation Methods

Direct Encoding

Variables:

$x=2, x=3, x=4, x=5, x=6$

Order Encoding

$x, y \in \{2..6\}$

Translation Methods

Direct Encoding

Variables:

$x=2, x=3, x=4, x=5, x=6$

At least one:

$x=2 \vee x=3 \vee x=4 \vee x=5 \vee$
 $x=6$

Order Encoding

$x, y \in \{2..6\}$

Translation Methods

Direct Encoding

Variables:

$x=2, x=3, x=4, x=5, x=6$

At least one:

$x=2 \vee x=3 \vee x=4 \vee x=5 \vee$
 $x=6$

At most one:

$\neg x=2 \vee \neg x=3, \neg x=2 \vee \neg x=4,$
 $\neg x=2 \vee \neg x=5, \neg x=2 \vee \neg x=6,$
 $\neg x=3 \vee \neg x=4, \neg x=3 \vee \neg x=5,$
 $\neg x=3 \vee \neg x=6,$
 $\neg x=4 \vee \neg x=5, \neg x=4 \vee \neg x=6,$
 $\neg x=5 \vee \neg x=6$

Order Encoding

$x, y \in \{2..6\}$

Translation Methods

Direct Encoding

Variables:

$x=2, x=3, x=4, x=5, x=6$

At least one:

$x=2 \vee x=3 \vee x=4 \vee x=5 \vee$
 $x=6$

At most one:

$\neg x=2 \vee \neg x=3, \neg x=2 \vee \neg x=4,$
 $\neg x=2 \vee \neg x=5, \neg x=2 \vee \neg x=6,$
 $\neg x=3 \vee \neg x=4, \neg x=3 \vee \neg x=5,$
 $\neg x=3 \vee \neg x=6,$
 $\neg x=4 \vee \neg x=5, \neg x=4 \vee \neg x=6,$
 $\neg x=5 \vee \neg x=6$

$x, y \in \{2..6\}$

Order Encoding

Variables:

$x \leq 2, x \leq 3, x \leq 4,$
 $x \leq 5, x \leq 6$

Translation Methods

Direct Encoding

Variables:

$x=2, x=3, x=4, x=5, x=6$

At least one:

$x=2 \vee x=3 \vee x=4 \vee x=5 \vee$
 $x=6$

At most one:

$\neg x=2 \vee \neg x=3, \neg x=2 \vee \neg x=4,$
 $\neg x=2 \vee \neg x=5, \neg x=2 \vee \neg x=6,$
 $\neg x=3 \vee \neg x=4, \neg x=3 \vee \neg x=5,$
 $\neg x=3 \vee \neg x=6,$
 $\neg x=4 \vee \neg x=5, \neg x=4 \vee \neg x=6,$
 $\neg x=5 \vee \neg x=6$

$x, y \in \{2..6\}$

Order Encoding

Variables:

$x \leq 2, x \leq 3, x \leq 4,$
 $x \leq 5, \cancel{x \leq 6}$

Translation Methods

Direct Encoding

Variables:

$x=2, x=3, x=4, x=5, x=6$

At least one:

$x=2 \vee x=3 \vee x=4 \vee x=5 \vee$
 $x=6$

At most one:

$\neg x=2 \vee \neg x=3, \neg x=2 \vee \neg x=4,$
 $\neg x=2 \vee \neg x=5, \neg x=2 \vee \neg x=6,$
 $\neg x=3 \vee \neg x=4, \neg x=3 \vee \neg x=5,$
 $\neg x=3 \vee \neg x=6,$
 $\neg x=4 \vee \neg x=5, \neg x=4 \vee \neg x=6,$
 $\neg x=5 \vee \neg x=6$

$x, y \in \{2..6\}$

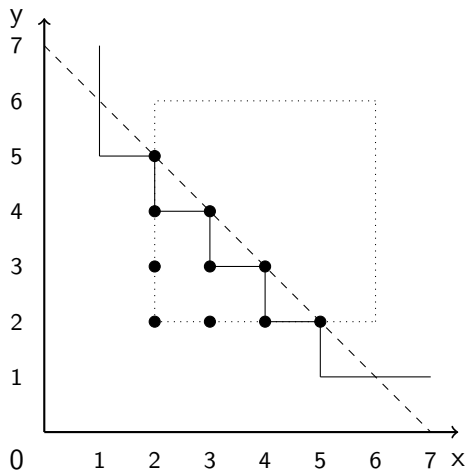
Order Encoding

Variables:

$x \leq 2, x \leq 3, x \leq 4,$
 $x \leq 5, \cancel{x \leq 6}$

At most one:

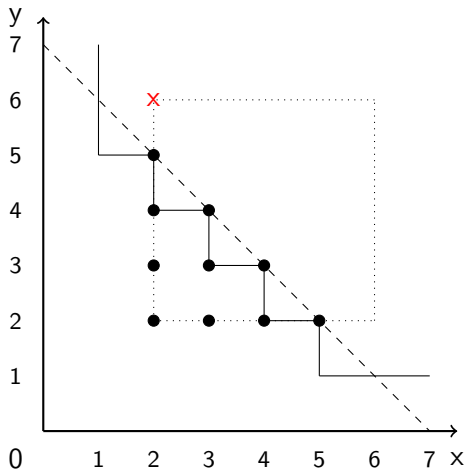
$\neg x \leq 2 \vee x \leq 3,$
 $\neg x \leq 3 \vee x \leq 4,$
 $\neg x \leq 4 \vee x \leq 5$

Translating $x + y \leq 7$ 

Direct Encoding
 $x \neq 2 \vee y \neq 6$

Translating $x + y \leq 7$

Order Encoding



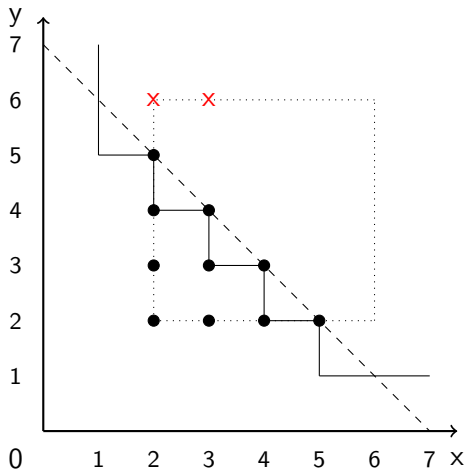
Direct Encoding

$$x \neq 2 \vee y \neq 6$$

$$x \neq 3 \vee y \neq 6$$

Translating $x + y \leq 7$

Order Encoding



Direct Encoding

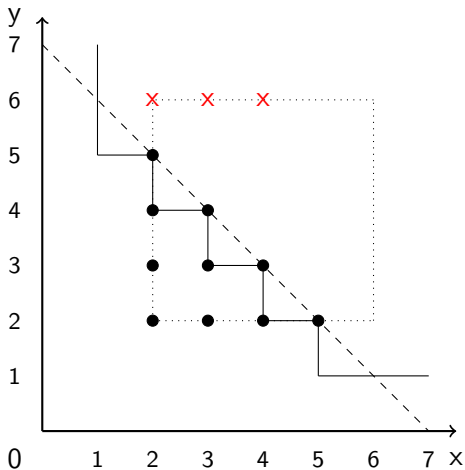
$$x \neq 2 \vee y \neq 6$$

$$x \neq 3 \vee y \neq 6$$

$$x \neq 4 \vee y \neq 6$$

Translating $x + y \leq 7$

Order Encoding



Direct Encoding

$$x \neq 2 \vee y \neq 6$$

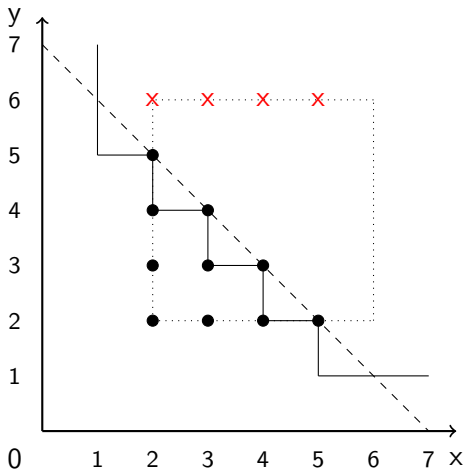
$$x \neq 3 \vee y \neq 6$$

$$x \neq 4 \vee y \neq 6$$

$$x \neq 5 \vee y \neq 6$$

Translating $x + y \leq 7$

Order Encoding



Direct Encoding

$$x \neq 2 \vee y \neq 6$$

$$x \neq 3 \vee y \neq 6$$

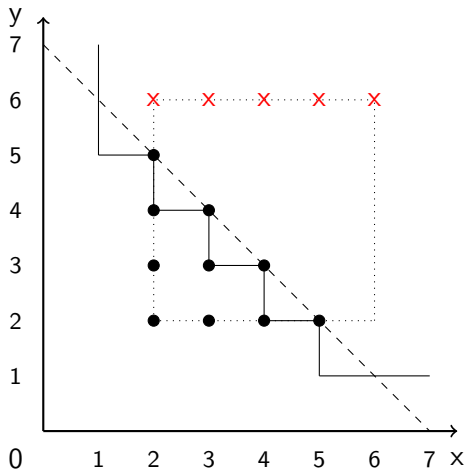
$$x \neq 4 \vee y \neq 6$$

$$x \neq 5 \vee y \neq 6$$

$$x \neq 6 \vee y \neq 6$$

Translating $x + y \leq 7$

Order Encoding



Direct Encoding

$$x \neq 2 \vee y \neq 6$$

$$x \neq 3 \vee y \neq 6$$

$$x \neq 4 \vee y \neq 6$$

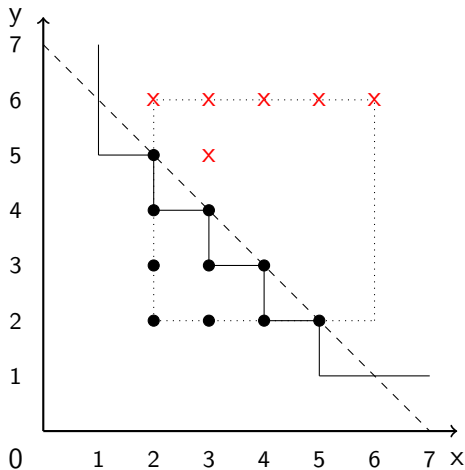
$$x \neq 5 \vee y \neq 6$$

$$x \neq 6 \vee y \neq 6$$

$$x \neq 3 \vee y \neq 5$$

Translating $x + y \leq 7$

Order Encoding



Direct Encoding

$$x \neq 2 \vee y \neq 6$$

$$x \neq 3 \vee y \neq 6$$

$$x \neq 4 \vee y \neq 6$$

$$x \neq 5 \vee y \neq 6$$

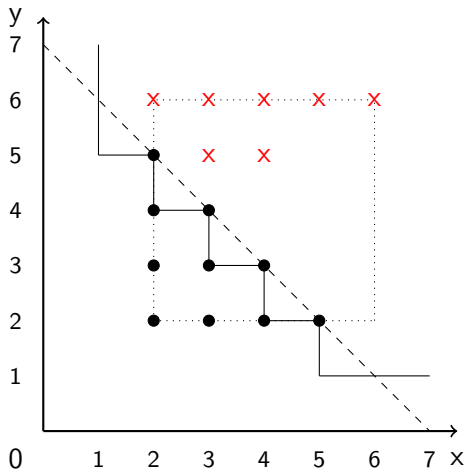
$$x \neq 6 \vee y \neq 6$$

$$x \neq 3 \vee y \neq 5$$

$$x \neq 4 \vee y \neq 5$$

Translating $x + y \leq 7$

Order Encoding



Direct Encoding

$$x \neq 2 \vee y \neq 6$$

$$x \neq 3 \vee y \neq 6$$

$$x \neq 4 \vee y \neq 6$$

$$x \neq 5 \vee y \neq 6$$

$$x \neq 6 \vee y \neq 6$$

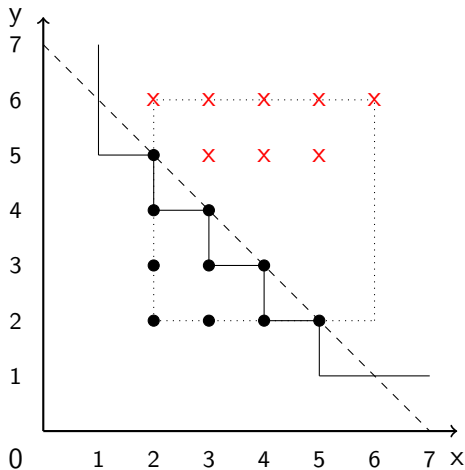
$$x \neq 3 \vee y \neq 5$$

$$x \neq 4 \vee y \neq 5$$

$$x \neq 5 \vee y \neq 5$$

Translating $x + y \leq 7$

Order Encoding



Direct Encoding

$$x \neq 2 \vee y \neq 6$$

$$x \neq 3 \vee y \neq 6$$

$$x \neq 4 \vee y \neq 6$$

$$x \neq 5 \vee y \neq 6$$

$$x \neq 6 \vee y \neq 6$$

$$x \neq 3 \vee y \neq 5$$

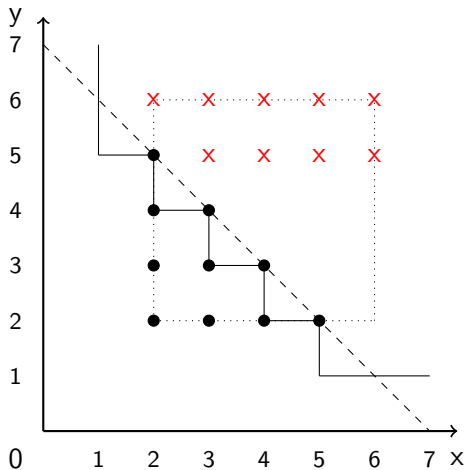
$$x \neq 4 \vee y \neq 5$$

$$x \neq 5 \vee y \neq 5$$

$$x \neq 6 \vee y \neq 5$$

Translating $x + y \leq 7$

Order Encoding



Direct Encoding

$$x \neq 2 \vee y \neq 6$$

$$x \neq 3 \vee y \neq 6$$

$$x \neq 4 \vee y \neq 6$$

$$x \neq 5 \vee y \neq 6$$

$$x \neq 6 \vee y \neq 6$$

$$x \neq 3 \vee y \neq 5$$

$$x \neq 4 \vee y \neq 5$$

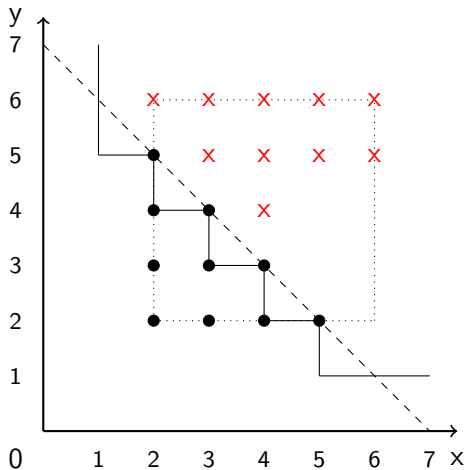
$$x \neq 5 \vee y \neq 5$$

$$x \neq 6 \vee y \neq 5$$

$$x \neq 4 \vee y \neq 4$$

Translating $x + y \leq 7$

Order Encoding



Direct Encoding

$$x \neq 2 \vee y \neq 6$$

$$x \neq 3 \vee y \neq 6$$

$$x \neq 4 \vee y \neq 6$$

$$x \neq 5 \vee y \neq 6$$

$$x \neq 6 \vee y \neq 6$$

$$x \neq 3 \vee y \neq 5$$

$$x \neq 4 \vee y \neq 5$$

$$x \neq 5 \vee y \neq 5$$

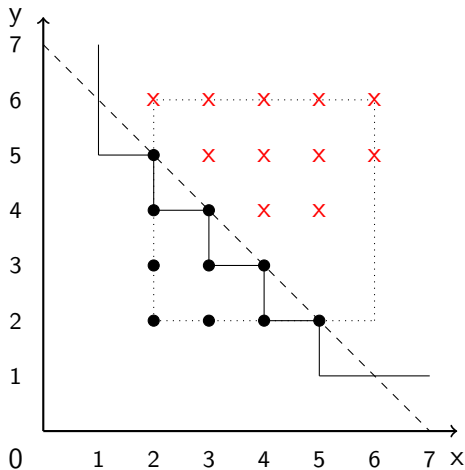
$$x \neq 6 \vee y \neq 5$$

$$x \neq 4 \vee y \neq 4$$

$$x \neq 5 \vee y \neq 4$$

Translating $x + y \leq 7$

Order Encoding



Direct Encoding

$$x \neq 2 \vee y \neq 6$$

$$x \neq 3 \vee y \neq 6$$

$$x \neq 4 \vee y \neq 6$$

$$x \neq 5 \vee y \neq 6$$

$$x \neq 6 \vee y \neq 6$$

$$x \neq 3 \vee y \neq 5$$

$$x \neq 4 \vee y \neq 5$$

$$x \neq 5 \vee y \neq 5$$

$$x \neq 6 \vee y \neq 5$$

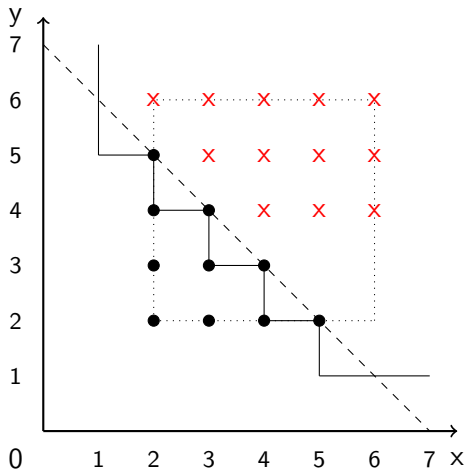
$$x \neq 4 \vee y \neq 4$$

$$x \neq 5 \vee y \neq 4$$

$$x \neq 6 \vee y \neq 4$$

Translating $x + y \leq 7$

Order Encoding



Direct Encoding

$$x \neq 2 \vee y \neq 6$$

$$x \neq 3 \vee y \neq 6$$

$$x \neq 4 \vee y \neq 6$$

$$x \neq 5 \vee y \neq 6$$

$$x \neq 6 \vee y \neq 6$$

$$x \neq 3 \vee y \neq 5$$

$$x \neq 4 \vee y \neq 5$$

$$x \neq 5 \vee y \neq 5$$

$$x \neq 6 \vee y \neq 5$$

$$x \neq 4 \vee y \neq 4$$

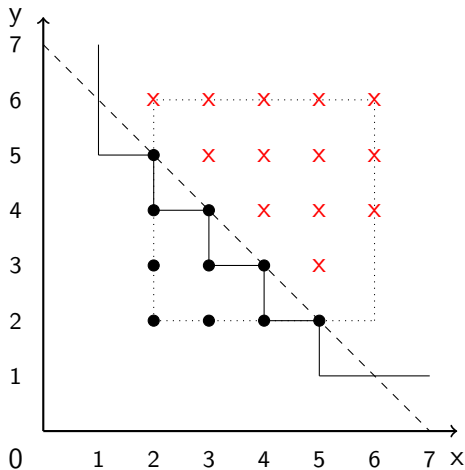
$$x \neq 5 \vee y \neq 4$$

$$x \neq 6 \vee y \neq 4$$

$$x \neq 5 \vee y \neq 3$$

Translating $x + y \leq 7$

Order Encoding



Direct Encoding

$$x \neq 2 \vee y \neq 6$$

$$x \neq 3 \vee y \neq 6$$

$$x \neq 4 \vee y \neq 6$$

$$x \neq 5 \vee y \neq 6$$

$$x \neq 6 \vee y \neq 6$$

$$x \neq 3 \vee y \neq 5$$

$$x \neq 4 \vee y \neq 5$$

$$x \neq 5 \vee y \neq 5$$

$$x \neq 6 \vee y \neq 5$$

$$x \neq 4 \vee y \neq 4$$

$$x \neq 5 \vee y \neq 4$$

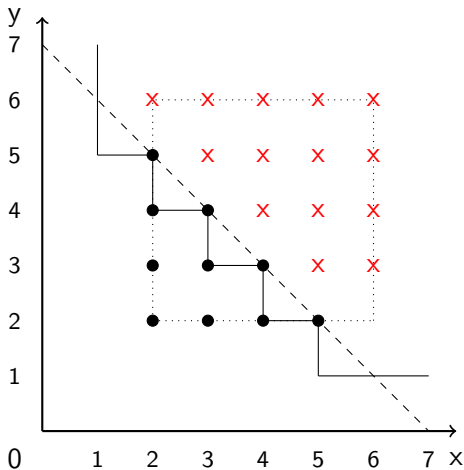
$$x \neq 6 \vee y \neq 4$$

$$x \neq 5 \vee y \neq 3$$

$$x \neq 6 \vee y \neq 3$$

Translating $x + y \leq 7$

Order Encoding



Direct Encoding

$$x \neq 2 \vee y \neq 6$$

$$x \neq 3 \vee y \neq 6$$

$$x \neq 4 \vee y \neq 6$$

$$x \neq 5 \vee y \neq 6$$

$$x \neq 6 \vee y \neq 6$$

$$x \neq 3 \vee y \neq 5$$

$$x \neq 4 \vee y \neq 5$$

$$x \neq 5 \vee y \neq 5$$

$$x \neq 6 \vee y \neq 5$$

$$x \neq 4 \vee y \neq 4$$

$$x \neq 5 \vee y \neq 4$$

$$x \neq 6 \vee y \neq 4$$

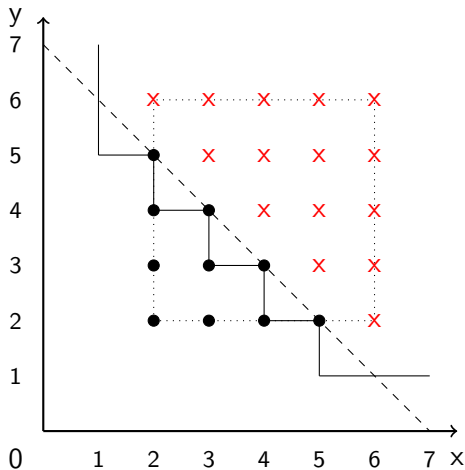
$$x \neq 5 \vee y \neq 3$$

$$x \neq 6 \vee y \neq 3$$

$$x \neq 6 \vee y \neq 2$$

Translating $x + y \leq 7$

Order Encoding



Direct Encoding

$$x \neq 2 \vee y \neq 6$$

$$x \neq 3 \vee y \neq 6$$

$$x \neq 4 \vee y \neq 6$$

$$x \neq 5 \vee y \neq 6$$

$$x \neq 6 \vee y \neq 6$$

$$x \neq 3 \vee y \neq 5$$

$$x \neq 4 \vee y \neq 5$$

$$x \neq 5 \vee y \neq 5$$

$$x \neq 6 \vee y \neq 5$$

$$x \neq 4 \vee y \neq 4$$

$$x \neq 5 \vee y \neq 4$$

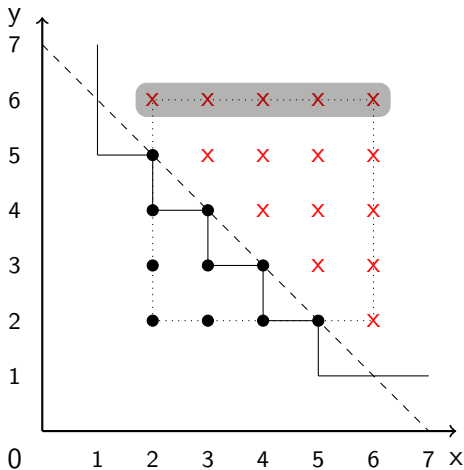
$$x \neq 6 \vee y \neq 4$$

$$x \neq 5 \vee y \neq 3$$

$$x \neq 6 \vee y \neq 3$$

$$x \neq 6 \vee y \neq 2$$

Translating $x + y \leq 7$



Order Encoding

$$x \leq 1 \vee y \leq 5$$

Direct Encoding

$$x \neq 2 \vee y \neq 6$$

$$x \neq 3 \vee y \neq 6$$

$$x \neq 4 \vee y \neq 6$$

$$x \neq 5 \vee y \neq 6$$

$$x \neq 6 \vee y \neq 6$$

$$x \neq 3 \vee y \neq 5$$

$$x \neq 4 \vee y \neq 5$$

$$x \neq 5 \vee y \neq 5$$

$$x \neq 6 \vee y \neq 5$$

$$x \neq 4 \vee y \neq 4$$

$$x \neq 5 \vee y \neq 4$$

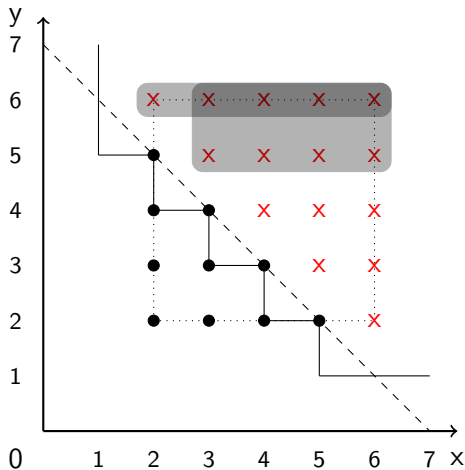
$$x \neq 6 \vee y \neq 4$$

$$x \neq 5 \vee y \neq 3$$

$$x \neq 6 \vee y \neq 3$$

$$x \neq 6 \vee y \neq 2$$

Translating $x + y \leq 7$



Order Encoding

$$x \leq 1 \vee y \leq 5$$

$$x \leq 2 \vee y \leq 4$$

Direct Encoding

$$x \neq 2 \vee y \neq 6$$

$$x \neq 3 \vee y \neq 6$$

$$x \neq 4 \vee y \neq 6$$

$$x \neq 5 \vee y \neq 6$$

$$x \neq 6 \vee y \neq 6$$

$$x \neq 3 \vee y \neq 5$$

$$x \neq 4 \vee y \neq 5$$

$$x \neq 5 \vee y \neq 5$$

$$x \neq 6 \vee y \neq 5$$

$$x \neq 4 \vee y \neq 4$$

$$x \neq 5 \vee y \neq 4$$

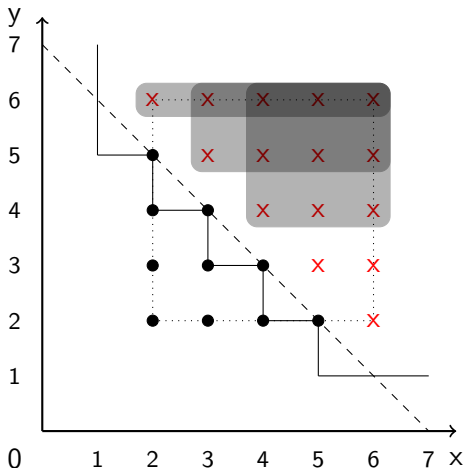
$$x \neq 6 \vee y \neq 4$$

$$x \neq 5 \vee y \neq 3$$

$$x \neq 6 \vee y \neq 3$$

$$x \neq 6 \vee y \neq 2$$

Translating $x + y \leq 7$



Order Encoding

$$x \leq 1 \vee y \leq 5$$

$$x \leq 2 \vee y \leq 4$$

$$x \leq 3 \vee y \leq 3$$

Direct Encoding

$$x \neq 2 \vee y \neq 6$$

$$x \neq 3 \vee y \neq 6$$

$$x \neq 4 \vee y \neq 6$$

$$x \neq 5 \vee y \neq 6$$

$$x \neq 6 \vee y \neq 6$$

$$x \neq 3 \vee y \neq 5$$

$$x \neq 4 \vee y \neq 5$$

$$x \neq 5 \vee y \neq 5$$

$$x \neq 6 \vee y \neq 5$$

$$x \neq 4 \vee y \neq 4$$

$$x \neq 5 \vee y \neq 4$$

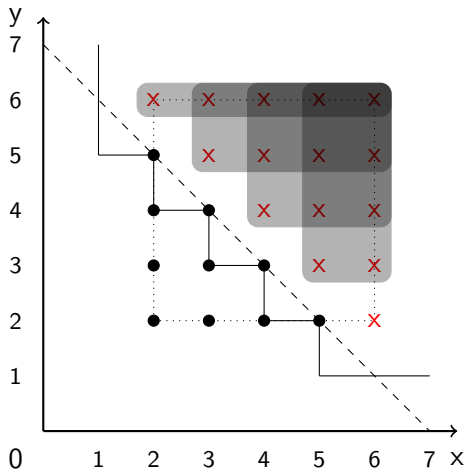
$$x \neq 6 \vee y \neq 4$$

$$x \neq 5 \vee y \neq 3$$

$$x \neq 6 \vee y \neq 3$$

$$x \neq 6 \vee y \neq 2$$

Translating $x + y \leq 7$



Order Encoding

$$x \leq 1 \vee y \leq 5$$

$$x \leq 2 \vee y \leq 4$$

$$x \leq 3 \vee y \leq 3$$

$$x \leq 4 \vee y \leq 2$$

Direct Encoding

$$x \neq 2 \vee y \neq 6$$

$$x \neq 3 \vee y \neq 6$$

$$x \neq 4 \vee y \neq 6$$

$$x \neq 5 \vee y \neq 6$$

$$x \neq 6 \vee y \neq 6$$

$$x \neq 3 \vee y \neq 5$$

$$x \neq 4 \vee y \neq 5$$

$$x \neq 5 \vee y \neq 5$$

$$x \neq 6 \vee y \neq 5$$

$$x \neq 4 \vee y \neq 4$$

$$x \neq 5 \vee y \neq 4$$

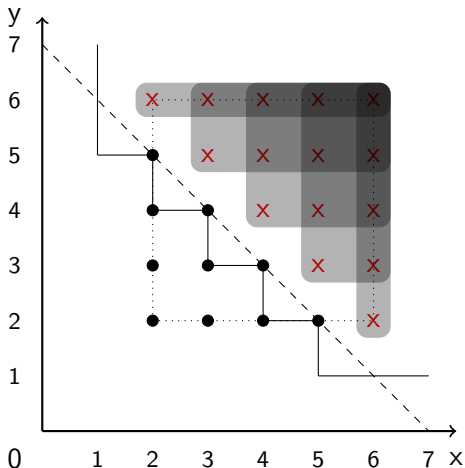
$$x \neq 6 \vee y \neq 4$$

$$x \neq 5 \vee y \neq 3$$

$$x \neq 6 \vee y \neq 3$$

$$x \neq 6 \vee y \neq 2$$

Translating $x + y \leq 7$



Order Encoding

$$x \leq 1 \vee y \leq 5$$

$$x \leq 2 \vee y \leq 4$$

$$x \leq 3 \vee y \leq 3$$

$$x \leq 4 \vee y \leq 2$$

$$x \leq 5 \vee y \leq 1$$

Tasks

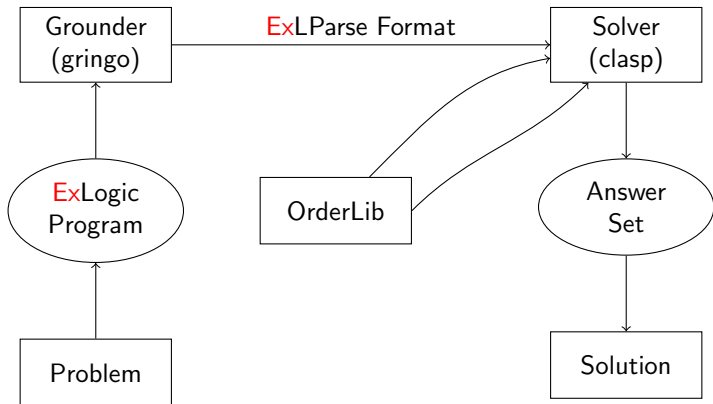
- storing constraints and variables
- preprocessing
- propagation w/wo reasoning
- translation

Tasks

- storing constraints and variables
- preprocessing
- propagation w/wo reasoning
- translation



What to do with it?



Features

Make it nice!

- order variables + direct variables on demand
- equality processing
- domain constraints
- disjoint constraints
- alldifferent constraints
 - simple pairwise equality
 - scaleable hall intervals (exponential, better propagation)
 - pidgeon hole optimization

Features

Make it nice!

- order variables + direct variables on demand
- equality processing
- domain constraints
- disjoint constraints
- alldifferent constraints
 - simple pairwise equality
 - scaleable hall intervals (exponential, better propagation)
 - pidgeon hole optimization

Features

Make it nice!

- order variables + direct variables on demand
- equality processing
- domain constraints
- disjoint constraints
- alldifferent constraints
 - simple pairwise equality
 - scaleable hall intervals (exponential, better propagation)
 - pidgeon hole optimization

Features

Make it nice!

- order variables + direct variables on demand
- equality processing
- domain constraints
- disjoint constraints
- alldifferent constraints
 - simple pairwise equality
 - scaleable hall intervals (exponential, better propagation)
 - pidgeon hole optimization

Features

Make it nice!

- order variables + direct variables on demand
- equality processing
- domain constraints
- disjoint constraints
- alldifferent constraints
 - simple pairwise equality
 - scaleable hall intervals (exponential, better propagation)
 - pidgeon hole optimization

More Features

Make it nicer!

- **splitting**
- heuristic domain propagation
- symmetry breaking
 - using projection ?
 - computing only 1 model
- redundant clause check

Splitting

Exponential Translation

$$x_1 + x_2 + x_3 + \dots + x_{22} \leq 13864$$

Quadratic Translation

$$x_1 + x_2 = v_1$$

$$x_3 + x_4 = v_2$$

...

$$v_1 + v_2 = w_1$$

...

$$w_1 + w_2 \leq 13864$$

More Features

Make it nicer!

- splitting
- heuristic domain propagation
- symmetry breaking
 - using projection ?
 - computing only 1 model
- redundant clause check

Heuristic Domain Propagation

Bound Propagation

$$0 \leq x \leq 1$$

$$0 \leq y \leq 1$$

$$42x + 1337y = v$$

$$0 \leq v \leq 1379$$

Domain Propagation

$$v = \{0, 42, 1337, 1379\}$$

Heuristic Domain Propagation

Bound Propagation

$$0 \leq x \leq 1$$

$$0 \leq y \leq 1$$

$$42x + 1337y = v$$

$$0 \leq v \leq 1379$$

Domain Propagation

$$v = \{0, 42, 1337, 1379\}$$

Heuristic Domain Propagation

Bound Propagation

$$0 \leq x \leq 1$$

$$0 \leq y \leq 1$$

$$42x + 1337y = v$$

$$0 \leq v \leq 1379$$

Domain Propagation

$$v = \{0, 42, 1337, 1379\}$$

More Features

Make it nicer!

- splitting
- heuristic domain propagation
- symmetry breaking
 - using projection ?
 - computing only 1 model
- redundant clause check

Symmetry Breaking

Splitting

$$x_1 + x_2 + x_3 + \cdots + x_{22} \leq 13864$$

Quadratic Translation

$$x_1 + x_2 = v_1$$

$$x_3 + x_4 = v_2$$

...

$$v_1 + v_2 = w_1$$

...

$$w_1 + w_2 \leq 13864$$

Symmetry Breaking

Splitting

$$x_1 + x_2 + x_3 + \cdots + x_{22} \leq 13864$$

Quadratic Translation

$$x_1 + x_2 \leq v_1$$

$$x_3 + x_4 \leq v_2$$

...

$$v_1 + v_2 \geq w_1$$

...

$$w_1 + w_2 \leq 13864$$

Symmetry Breaking

Splitting

$$x_1 + x_2 + x_3 + \cdots + x_{22} \leq 13864$$

Quadratic Translation

$$x_1 + x_2 \leq v_1$$

$$x_3 + x_4 \leq v_2$$

...

$$v_1 + v_2 \geq w_1$$

...

$$w_1 + w_2 \leq 13864$$

Project away additional solutions

More Features

Make it nicer!

- splitting
- heuristic domain propagation
- symmetry breaking
 - using projection ?
 - computing only 1 model
- redundant clause check

More Features

Make it perfect!

- propagator for order literals
- lazy clause generation
- lazy variable creation
- difference logic propagator
- ...

Overview

1 General Theory Language

2 SAT Modulo Theories

3 OrderLib

4 Example Evaluation

SendMoreMoney

1000s + 100e + 10n + 1d +
1000m + 100o + 10r + 1e =
10000m + 1000o + 100n + 10e + 1y.

alldistinct{s,e,n,d,m,o,r,y}.

- Ol' gringo: timeout/memout
- newgringo: 4500 vars, 1000 constraints, 0 seconds
- (hopefully) compareable to state of the art CSP systems

SendMoreMoney

1000s + 100e + 10n + 1d +
1000m + 100o + 10r + 1e =
10000m + 1000o + 100n + 10e + 1y.

alldistinct{s,e,n,d,m,o,r,y}.

- Ol' gringo: timeout/memout
- newgringo: 4500 vars, 1000 constraints, 0 seconds
- (hopefully) compareable to state of the art CSP systems

SendMoreMoney

1000s + 100e + 10n + 1d +
1000m + 100o + 10r + 1e =
10000m + 1000o + 100n + 10e + 1y.

alldistinct{s,e,n,d,m,o,r,y}.

- Ol' gringo: timeout/memout
- newgringo: 4500 vars, 1000 constraints, 0 seconds
- (hopefully) compareable to state of the art CSP systems

SendMoreMoney

1000s + 100e + 10n + 1d +
1000m + 100o + 10r + 1e =
10000m + 1000o + 100n + 10e + 1y.

alldistinct{s,e,n,d,m,o,r,y}.

- Ol' gringo: timeout/memout
- newgringo: 4500 vars, 1000 constraints, 0 seconds
- (hopefully) compareable to state of the art CSP systems

Large Domains

$$1440a + 6b - 3c = 136164$$

- $a, b, c = \{0..2^{30}\}$
- lazy clause and variable generation
- starting search with 0 constraints/variables
- generates 80 variables on the fly

Questions?

Thanks for your attention

CSP Competition

549 instances from global category

- OrderLib: 85(23) timeouts, 177.000s
- OldGringo: 267(172) timeouts, 497.000s
- Clingcon: 209(0) timeouts, 411.000s
- Sugar: 70(11) timeouts, 137.000s

CSP Competition

549 instances from global category

- OrderLib: 85(23) timeouts, 177.000s
- OldGringo: 267(172) timeouts, 497.000s
- Clingcon: 209(0) timeouts, 411.000s
- Sugar: 70(11) timeouts, 137.000s

CSP Competition

549 instances from global category

- OrderLib: 85(23) timeouts, 177.000s
- OldGringo: 267(172) timeouts, 497.000s
- Clingcon: 209(0) timeouts, 411.000s
- Sugar: 70(11) timeouts, 137.000s

CSP Competition

549 instances from global category

- OrderLib: 85(23) timeouts, 177.000s
- OldGringo: 267(172) timeouts, 497.000s
- Clingcon: 209(0) timeouts, 411.000s
- Sugar: 70(11) timeouts, 137.000s

Cheating

No gringo timeouts/sugar trans

- OrderLib: 66(4) timeouts, 143.000s
- OldGringo: 248(153) timeouts, 462.000s
- Clingcon: 197(0) timeouts, 489.000s
- Sugar: 64(11) timeouts, 125.000s

Cheating

No gringo timeouts/sugar trans

- OrderLib: 66(4) timeouts, 143.000s
- OldGringo: 248(153) timeouts, 462.000s
- **Clingcon: 197(0) timeouts, 489.000s**
- Sugar: 64(11) timeouts, 125.000s