

Predictive Runtime Enforcement

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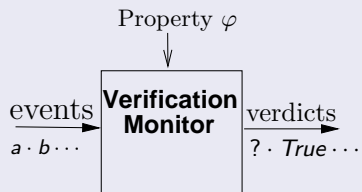
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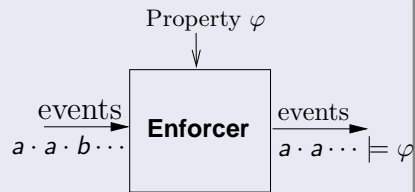
Runtime verification and enforcement

Runtime verification



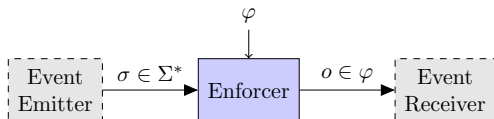
- Does σ satisfy φ ?
- Output: stream of **verdicts**.

Runtime enforcement

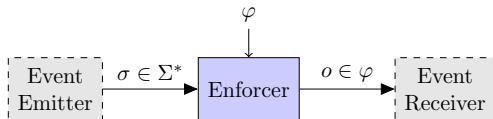


- Input: stream of events.
- **Modified** to satisfy the property.
- Output: stream of **events**.

Runtime enforcement (previous work: **non-predictive**)



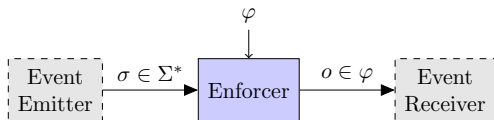
Runtime enforcement (previous work: **non-predictive**)



Enforcer for φ operating at runtime

- φ : any regular property (defined as automaton).

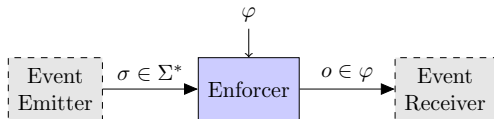
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- An enforcer behaves as a function $E : \Sigma^* \rightarrow \Sigma^*$.
 - Input ($\sigma \in \Sigma^*$): any sequence of events over Σ (Event emitter is a **black-box**).

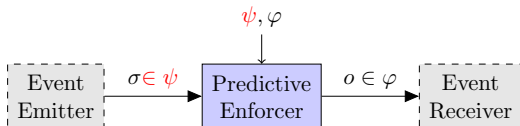
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 - Output ($o \in \Sigma^*$): a sequence of events such that $o \models \varphi$.

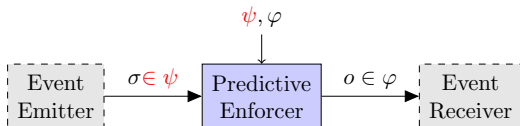
Predictive runtime enforcement problem (this work)



Predictive enforcer for φ operating at runtime

- Given property φ (to enforce) and **input property ψ** defined as automaton.
- Automatically synthesize an enforcer.

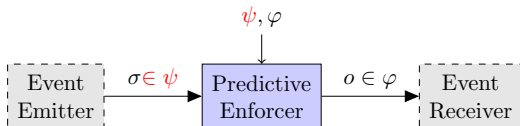
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Predictive runtime enforcement problem (this work)



Predictive enforcer for φ operating at runtime

- Given property φ (to enforce) and **input property** ψ defined as automaton.
- Automatically synthesize an enforcer.
 - Input ($\sigma \in \psi$): Event emitter is not a black-box.
 - Output ($o \in \Sigma^*$): a sequence of events $o \models \varphi$.
 - Predictive enforcer should satisfy soundness, transparency, monotonicity, and **urgency** constraints.
 - Urgency related to using ψ and release input events earlier whenever possible.

Predictive runtime enforcement (motivations)

Motivations

- Consider a-priori knowledge of the system (event emitter) is available.
 - Model, information extracted using static-analysis etc.
- Provide a-priori knowledge of the system (event emitter) to the enforcer.
 - Event emitter is not a black-box.
 - How enforcer can benefit from model/knowledge of the system?
 - Does it help to provide better QoS (eg: output some events earlier)?

Example

- Non-safety properties (release events earlier instead of delaying).

Related works

Runtime Enforcement: non-predictive

- Enforceable security policies – [F. B. Schneider et al-2000](#).
- Runtime enforcement of non-safety policies – [J. Ligatti et al-2009](#).
- Enforcement monitoring wrt. the safety-progress classification of properties – [Y. Falcone et al-2010](#).
- Runtime enforcement of timed properties – [S. Pinisetty et al-2012](#).
- Runtime enforcement for reactive systems – [R. Bloem et al-2015](#).

Outline

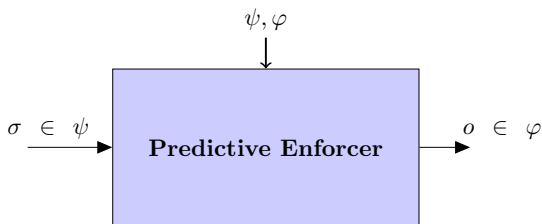
- 1 Introduction
- 2 Formal Problem Definition
- 3 Automatic Enforcer Synthesis
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Predictive enforcer

Given properties ψ (input property) and φ (to enforce):



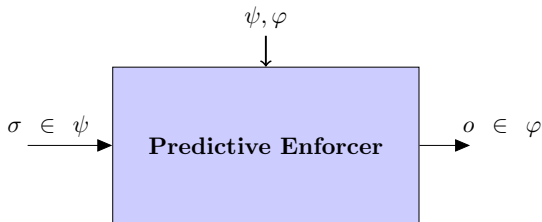
What can an enforcer do?

Enforcer augmented with a **memorization mechanism**.

- **CAN** delay events.
- **CANNOT** insert nor delete events.
- **CANNOT** change the order of events.

Formal problem definition

Properties ψ (input property) and φ (to enforce).



Predictive enforcer for ψ, φ

Given properties $\psi, \varphi \subseteq \Sigma^*$, a *predictive enforcer* is a function $E_{\psi, \varphi} : \Sigma^* \rightarrow \Sigma^*$ satisfying the following constraints:

- 1 Soundness
- 2 Transparency
- 3 Monotonicity
- 4 **Urgency**

Soundness

Output is correct (satisfies φ)

$$\forall \sigma \in \psi : E_{\psi, \varphi}(\sigma) \neq \epsilon \implies E_{\psi, \varphi}(\sigma) \in \varphi.$$

Transparency

TR1: events can be delayed

$$\forall \sigma \in \Sigma^* : E_{\psi, \varphi}(\sigma) \preceq \sigma.$$

Transparency

TR1: events can be delayed

$$\forall \sigma \in \Sigma^* : E_{\psi, \varphi}(\sigma) \preceq \sigma.$$

TR2: observed input satisfies φ

$$\forall \sigma \in \Sigma^* : \sigma \in \varphi \implies E_{\psi, \varphi}(\sigma) = \sigma$$

Monotonicity

Modify output only by appending new events

$$\forall \sigma, \sigma' \in \Sigma^* : \sigma \preceq \sigma' \implies E_{\psi, \varphi}(\sigma) \preceq E_{\psi, \varphi}(\sigma')$$

Urgency

Release observed input ASAP predicting future input using ψ

$$\forall \sigma \in \Sigma^* : (\forall \sigma_{\text{con}} \in \Sigma^* : \sigma \cdot \sigma_{\text{con}} \in \psi \implies \\ \exists \sigma' \in \Sigma^* : \sigma' \preceq \sigma_{\text{con}} \wedge \sigma \cdot \sigma' \in \varphi) \implies E_{\psi, \varphi}(\sigma) = \sigma$$

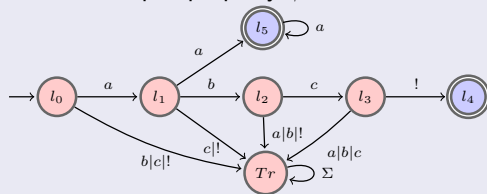
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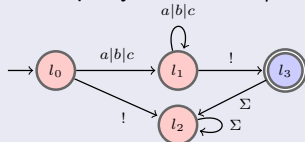
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Example

Input property ψ



Property to enforce φ



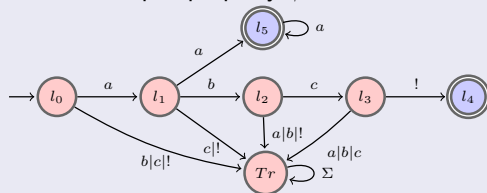
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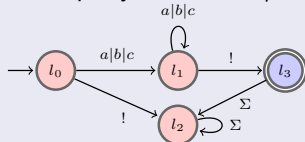
Example

Input property ψ



• $\sigma = a \notin \varphi$

Property to enforce φ



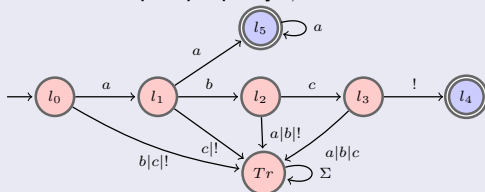
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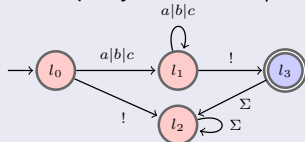
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Input property ψ



- $\sigma = a \notin \varphi$, $\sigma_{\text{con}} = \{b \cdot c \cdot !, a \cdot a \cdot a \cdots a\}$

Property to enforce φ



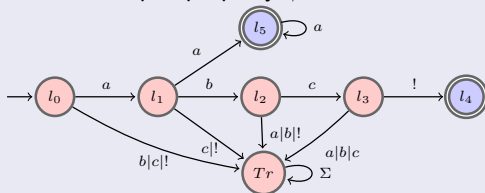
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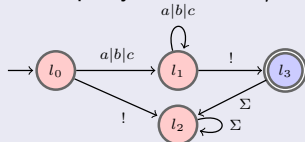
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Example

Input property ψ



Property to enforce φ



- $\sigma = a \notin \varphi$, $\sigma_{\text{con}} = \{b \cdot c \cdot !, a \cdot a \cdot a \cdots a\}$, **WAIT**.

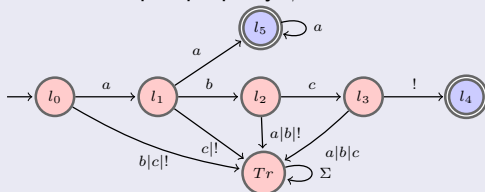
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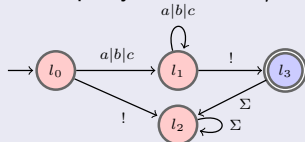
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Property to enforce φ



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- $\sigma = a \cdot b \notin \varphi$

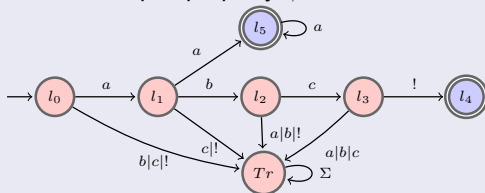
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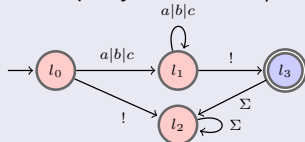
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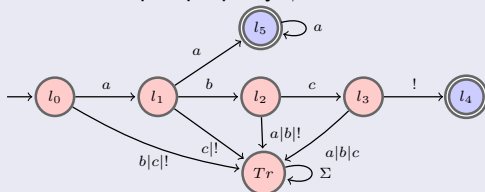
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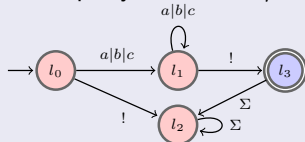
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Property to enforce φ



- $\sigma = a \notin \varphi$, $\sigma_{\text{con}} = \{b \cdot c \cdot !, a \cdot a \cdot a \cdots a\}$, **WAIT**.
- $\sigma = a \cdot b \notin \varphi$, $\sigma_{\text{con}} = \{c \cdot !\}$, **RELEASE** $a \cdot b$.

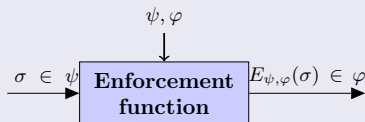
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Functional definition

$$E_{\psi, \varphi} : \Sigma^* \rightarrow \Sigma^*$$

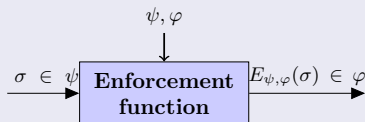
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Functional definition

$$E_{\psi,\varphi} : \Sigma^* \rightarrow \Sigma^*$$

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$$\text{store}_{\psi,\varphi} : \Sigma^* \rightarrow \Sigma^* \times \Sigma^*$$

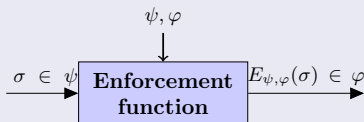
$\text{store}_{\psi,\varphi}(\sigma)$ is a pair:

- ① output of the enforcer (prefix of σ),
- ② suffix of σ which the enforcer cannot output yet.

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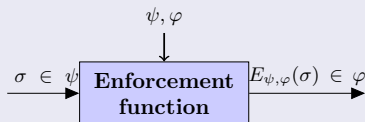
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Suppose $(\sigma_s, \sigma_c) = \text{store}_{\psi, \varphi}(\sigma)$

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Suppose $(\sigma_s, \sigma_c) = \text{store}_{\psi, \varphi}(\sigma)$

$$\text{store}_{\psi, \varphi}(\sigma \cdot a) = \begin{cases} (\sigma_s \cdot \sigma_c \cdot a, \epsilon) & \text{if } \kappa_{\psi, \varphi}(\sigma_s \cdot \sigma_c \cdot a), \\ (\sigma_s, \sigma_c \cdot a) & \text{otherwise} \end{cases}$$

where $\kappa_{\psi, \varphi}$ tests the hypothesis of the **Urgency** constraint.

Functional definition satisfies constraints

Theorem

The functional definition we previously saw satisfies the following constraints:

- 1 *Soundness*
- 2 *Transparency*
- 3 *Monotonicity*
- 4 *Urgency*

Isabelle proofs

<https://github.com/isabelle-theory/PredictiveRuntimeEnforcement>

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Enforcement algorithm

Input: $\mathcal{A}_\psi = (Q_\psi, q_\psi, \Sigma, \delta_\psi, F_\psi)$, $\mathcal{A}_\varphi = (Q_\varphi, q_\varphi, \Sigma, \delta_\varphi, F_\varphi)$.

Online algorithm

initialize memory, automata current states;

while *True* **do**

 WAIT for input event;

 UPDATE current states;

if $(\kappa_{\psi,\varphi}())$ **then**

 | RELEASE memory content and input event;

else

 | ADD input event to memory;

end

end

Implementation of $\kappa_{\psi,\varphi}$

Input: $\mathcal{A}_\psi = (Q_\psi, q_\psi, \Sigma, \delta_\psi, F_\psi)$, $\mathcal{A}_\varphi = (Q_\varphi, q_\varphi, \Sigma, \delta_\varphi, F_\varphi)$.

Testing $\kappa_{\psi,\varphi}(\sigma)$ by checking emptiness of a regular language

- p = state in \mathcal{A}_ψ upon reading σ .
- q = state in \mathcal{A}_φ upon reading σ .

$$\kappa_{\psi,\varphi}(\sigma) \iff \mathcal{L}(\mathcal{A}_\psi \times \overline{\mathcal{B}_\varphi}, (p, q)) = \emptyset$$

Implementation of $\kappa_{\psi, \varphi}$

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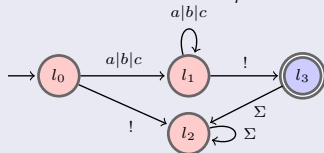
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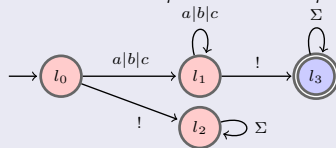
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Automaton B_φ

Automaton \mathcal{A}_φ .



Automaton B_φ based on \mathcal{A}_φ .



Enforcement algorithm

Predictive Enforcer

```
1:  $\sigma_c \leftarrow \epsilon$ 
2:  $p, q \leftarrow q_\psi, q_\varphi$ 
3:  $\mathcal{C} \leftarrow \mathcal{A}_\psi \times \overline{\mathcal{B}_\varphi}$ 
4: while true do
5:    $a \leftarrow \text{await\_event}()$ 
6:    $p, q \leftarrow \delta_\psi(p, a), \delta_\varphi(q, a)$ 
7:   if  $\mathcal{L}(\mathcal{C}, (p, q)) = \emptyset$  then
8:      $\text{release}(\sigma_c \cdot a)$ 
9:      $\sigma_c \leftarrow \epsilon$ 
10:  else
11:     $\sigma_c \leftarrow \sigma_c \cdot a$ 
12:  end if
13: end while
```

Complexity

- Product automaton \mathcal{C} , emptiness test for every state in \mathcal{C} (off-line).
- **Constant on-line time complexity.**

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 - A-priori knowledge of system behavior ψ .
 - Predicting future using ψ (**Urgency** constraint).
 - Urgency ensures that enforcer reacts ASAP.

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- Properties φ and ψ are regular languages (modeled as automata).
- Enforcer synthesis.
- Algorithms implementing these mechanisms in constant on-line time.
- Proofs in Isabelle.
- Implementation: <https://github.com/SrinivasPinisetty/PredictiveRE>.

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- Predictive RE for real-time properties.
- Implementation, case-studies.

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